# Bharatiya Vidya Bhavan's <br> Sardar Patel College of Engineering <br> (A Government Aided Autonomous Institute) <br> Munshi Nagar, Andheri (West), Mumbai - 400058. 

KT-Examination
June 2018

Duration: 3 hour
Class: S.Y.B.Tech Semester: III Program:Electrical Engineering
Name of the Course: Engineering Mathematics III Course Code : BTE201

- Question No. 1 is COMPULSORY
- Attempt any FOUR questions out of remaining SIX questions
- Answers to all sub questions should be grouped together.

| Q |  | Mar ks | CO | Module No. |
| :---: | :---: | :---: | :---: | :---: |
| 1(a) | Find the characteristic equation of the matrix A . $A=\left[\begin{array}{ccc}4 & 3 & -1 \\ 2 & 1 & -2 \\ 1 & 2 & 1\end{array}\right]$ Hence find $A^{-1}$ | 5 | 4 | 7 |
| (b) | Find Laplace transforms of $f(t)=\sin ^{3} t$ | 5 | 1 | 1 |
| (c) | Obtain the Fourier Series for $\mathrm{f}(\mathrm{x})= \begin{cases}0 & -2 \leq \mathrm{x} \leq-1 \\ 1+\mathrm{x} & -1 \leq \mathrm{x} \leq 0 \\ 1-\mathrm{x} & 0 \leq \mathrm{x} \leq 1 \\ 0 & 1 \leq \mathrm{x} \leq 2\end{cases}$ | 5 | 2 | 4 |


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| :---: | :---: | :---: | :---: | :---: |
| (d) | Show that the function $u(x, y)=4 x y-3 x+2$ is harmonic. Construct the corresponding analytic function $f(z)=u(x, y)+i v(x, y)$ | 5 | 3 | 5 |
| 2 (a) | Find the eigen values and eigen vectors of the matrix. $\left[\begin{array}{lll} 1 & 2 & 3 \\ 2 & 4 & 6 \\ 3 & 6 & 9 \end{array}\right]$ | 6 | 4 | 7 |
| (b) | Prove that $\int_{0}^{\infty} \frac{e^{-t} \sin ^{2} t}{t} d t=\frac{1}{4} \log 5$ | 6 | 1 | 2 |
| (c) | Obtain the half range sine series for $f(x)= \begin{cases}\frac{2 x}{3} & 0 \leq x \leq \frac{\pi}{3} \\ \frac{\pi-x}{3} & \frac{\pi}{3} \leq x \leq \pi\end{cases}$ | 8 | 2 | 5 |
| 3 (a) | Prove that the following function is analytic $f(z)=\operatorname{Sin}(z)$ | 6 | 3 | 5 |
| (b) | Show that $A=\left[\begin{array}{ccc}\cos 0 & 0 & \sin \theta \\ 0 & 1 & 0 \\ -\sin 0 & 0 & \cos \theta\end{array}\right]$ is an orthogonal matrix | 6 | 4 | 7 |
| (c) | Find $\mathrm{L}\left[\frac{d}{d t}\left(\frac{1-\cos 2 t}{t}\right)\right]$ | 8 | 1 | 1 |
| 4 (a) | Find the Fourier series for $f(x)=\left\{\begin{array}{lc}0 & -\pi \leq x \leq 0 \\ x^{2} & 0 \leq x \leq \pi\end{array}\right.$ | 6 | 2 | 4 |
| (b) | Find the Laplace transforms of $f(t)$, where $f(t)=\left\{\begin{array}{c} t, 0<t<1 \\ 0, t>1 \end{array}\right.$ | 6 | 1 | 1 |
| (c) | Find the analytic function $\mathrm{f}(\mathrm{z})=\mathrm{u}+\mathrm{iv}$, given that $u-v=(x-y)\left(x^{2}+4 x y+y^{2}\right)$ | 8 | 3 | 5 |
| 5 (a) | Evaluate: $\mathrm{L}^{-1}\left\{\begin{array}{l}2 \mathrm{~s}-1 \\ \mathrm{~s}^{3}+\mathrm{s}\end{array}\right\}$ | 6 | 1 | 2 |


| (b) | Find non - singular matrices $\mathrm{P}, \mathrm{Q}$ so that PAQ is a normal form where $A=\left[\begin{array}{ccc} 2 & 1 & 4 \\ 3 & 2 & 2 \\ 7 & 4 & 10 \\ 1 & 0 & 6 \end{array}\right]$ | 6 | 4 | 6 |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| (c) | Obtain complex form of the Fourier series for $f(x)=e^{-x} \quad-\pi \leq x \leq \pi$ | 8 | 2 | 4 |  |
| 6(a) | Evaluate: $L^{-1}\left\{\frac{s^{2}+2 s+3}{\left(s^{2}+2 s+5\right)\left(s^{2}+2 s+10\right)}\right\}$ | 6 | 1 | 2 |  |
| (b) | For what values of $\lambda$ and $\mu$ the linear equations. $\begin{aligned} & x+2 y+z=8 \\ & 2 x+2 y+2 z=13 \\ & 3 x+4 y+\lambda z=\mu \end{aligned}$ <br> have <br> i) No solution <br> ii) A unique solution <br> iii)infinite number of solutions | 6 | 4 | 6 |  |
| (c) | Show that the transform $w=\frac{1}{z}$ transforms circle $\|z-3\|=5$ into the circle. $\left\|w+\frac{3}{16}\right\|=\frac{5}{16}$ | 8 | 3 | 5 |  |
| 7 (a) | By using the sine series for $f(x)=1$ in $0<x<\pi$.Hence using parseval identity show that $\frac{\pi^{2}}{8}=1+\frac{1}{3^{2}}+\frac{1}{5^{2}}+\frac{1}{7^{2}}+\ldots$ | 6 | 2 | 4 |  |
| (b) | Evaluate: $\mathrm{L}^{-1}\left\{\log \left\|\frac{s-\mathrm{b}}{s-\mathrm{a}}\right\|\right\}$ | 6 | 1 | 2 |  |
| (c) | $\begin{aligned} \text { Solve } y \text { " }+\mathrm{y}= & \mathrm{t} \\ \text { Given } & \mathrm{y}(0)=1 \\ & y^{\prime}(0)=-2 \end{aligned}$ | 8 | 1 | 2 |  |

$$
\begin{aligned}
& \Leftrightarrow \text { Y Tech. Sem III BTE } 203 . \\
& \text { ELECTRICAL NETWORKS }
\end{aligned}
$$

Question no 1 is compulsory
Answer any 4 questions from the remaining 6
Assume suitable data if missing

1. Answer any four
a. Find z parameters of the following network.

b. Find the voltage across 5 ohm resistor in the circuit shown below

c. Draw the oriented graph and obtain the incidence matrix

d. Find $Z(S)$ and draw the pole zero plot for the network given below.

e. Synthesize the following driving point impedance function in Cauer-I form

$$
z(s)=\left(s^{2}+1\right) / s\left(s^{2}+3\right)
$$

2. a. For the network shown determine the current $I_{2}$ using superposition theorem

b. Determine y parameters for the following network

3. a. Find the incidence matrix, tie-set matrix and f-cutest matrix for the graph given below.

b. Test the following polynomials for Hurwitz
i) $P(s)=s^{4}+7 s^{3}+6 s^{2}+21 s+8$
ii) $P(s)=s^{4}+3 s^{2}+2$
iii) $P(s)=s^{5}+s^{3}+s$
4. a. Find $i\left(0^{+}\right), \operatorname{di}\left(0^{+}\right) / d t, d^{2} i\left(0^{+}\right) / d t^{2}$ if the switch is closed at $t=0$

b. Realize the following driving point function in Foster-I and Foster-II forms

$$
z(s)=s(s+3) /(s+1)(s+5)
$$

5. a. Find $V_{1}$ using nodal analysis

b. Draw the dual of the following network.
c. Test whether the following function is positive real
$(s)=\frac{2 s^{2}+2 s+1}{s^{3}+2 s^{2}+s+2}$

6. a. The switch is closed at $t=0$ Find $i(t)$ for $t>0$ using Laplace Transform.

The input is a Unit ramp function

b. A series RLC circuit has $R=10 \mathrm{ohms}, \mathrm{L}=\mathbf{6 0 \mathrm { mH }}$. At a frequency of $\mathbf{2 5 ~ H z}$ the [05] power factor of the circuit is $45^{\circ}$ lead. At what frequency does the circuit resonate?
c. In a series $R L C$ circuit $R=200 \Omega, L=0.1 H \& C=10 \mu F$ check whether the circuit is [05] under damped, critically damped or over damped.
7. a. Determine $V_{2} / V_{1}$ and $I_{1} / V_{2}$ for the network shown in figure.

b. Find the load impedance such that the maximum power is transferred to the load.

c. Derive the expression for current and voltage across a capacitor and plot current and voltage as a function of time.

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## Re Examination

Program: Electrical Engineering
Duration: 3 hrs.
Maximum Marks: 100

Date: June 2018
Course code: BTE 205
Semester: III

## Course Name: Electrical Machines I

Note: Answer any FIVE questions out of SEVEN.
Assume any suitable data if necessary and justify them.

1
a) Define and state the units of following parameters:
i) Magnetic flux
(ii) Magnetic flux density
iii) Magnetic field strength
(iv) Permeability
b)


What do you mean by electromechanical energy conversion? Fig. shows the magnetization characteristics, What does Area 10 oabo and Area abcda represent?

2 a) Discuss in detail all the conditions required for successful parallel operation of two transformers. How they will share the load?
b) A. $5 \mathrm{kVA}, 1000 / 200 \mathrm{~V}, 50 \mathrm{~Hz}$ single phase transformer gave following results:

OC Test (LV side): 200V, 1.2A, 90W
SC Test (HV side): 50V, 5A, 110W
Compute the parameters of approximate equivalent circuit referred to LV side. Also calculate the efficiency at half load and 0.8 pf lagging.

3 a) Compare two winding transformer with autotransformer and derive the 10 expression for copper saving in autotransformer.
b) A 125 kVA transformer with primary voltage of 2000 V at 50 Hz has 182 primary and 40 secondary turns. Neglecting losses, calculate a) full load primary and secondary currents $b$ ) no load secondary induced emf $c$ ) maximum 10 flux in core.
b) What is switching inrush current? Explain switching in phenomena of a three phase transformer 10

5 a) Illustrate with neat sketches cogging and crawling of induction motor $\quad 10$
b) Draw and explain the speed torque characteristics of a three phase induction motor and mark starting torque, maximum torque and full load operating point. 10

6 a) Why a starter is required for a three phase induction motor? Explain star delta 10 starter.
b) Explain the principle of operation of an induction generator. Where it is normally used?

7 a) Discuss briefly the effects of armature reaction with neat sketches. 10
b) Draw and explain torque-armature current, speed-torque and speed-armature current characteristics of DC shunt and series motor.

